# Markscheme 

## November 2020

## Mathematics

## Standard level

## Paper 2

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## Instructions to Examiners

## Abbreviations

M Marks awarded for attempting to use a valid Method; working must be seen.
(M) Marks awarded for a valid Method; may be implied by correct subsequent working.

A Marks awarded for an Answer or for Accuracy; often dependent on preceding M marks.
(A) Marks awarded for an Answer or for Accuracy; may be implied by correct subsequent working.
$\boldsymbol{R} \quad$ Marks awarded for clear Reasoning.
N Marks awarded for correct answers if no working shown.
AG Answer given in the question and so no marks are awarded.

## Using the markscheme

1 General
Mark according to RM assessor instructions.

## 2 Method and Answer/Accuracy marks

- Do not automatically award full marks for a correct answer; all working must be checked, and marks awarded according to the markscheme.
- It is generally not possible to award MO followed by $\boldsymbol{A 1}$, as $\boldsymbol{A}$ mark(s) depend on the preceding $\boldsymbol{M}$ mark(s), if any. An exception to this rule is when work for $\boldsymbol{M 1}$ is missing, as opposed to incorrect (see point 4).
- Where $\boldsymbol{M}$ and $\boldsymbol{A}$ marks are noted on the same line, eg M1A1, this usually means $\boldsymbol{M 1}$ for an attempt to use an appropriate method (eg substitution into a formula) and $\boldsymbol{A 1}$ for using the correct values.
- Where there are two or more $\boldsymbol{A}$ marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award A0A1A1.
- Where the markscheme specifies (M2), N3, etc., do not split the marks, unless there is a note.
- Most $\boldsymbol{M}$ marks are for a valid method, ie a method which can lead to the answer: it must indicate some form of progress towards the answer.
- Once a correct answer to a question or part-question is seen, ignore further correct working. However, if further working indicates a lack of mathematical understanding do not award final A1.


## $N$ marks

If no working shown, award $\mathbf{N}$ marks for correct answers. In this case, ignore mark breakdown ( $M, A, R$ ).

- Do not award a mixture of $\boldsymbol{N}$ and other marks.
- There may be fewer $\boldsymbol{N}$ marks available than the total of $\boldsymbol{M}, \boldsymbol{A}$ and $\boldsymbol{R}$ marks; this is deliberate as it penalizes candidates for not following the instruction to show their working.
- There may not be a direct relationship between the $\boldsymbol{N}$ marks and the implied marks. There are times when all the marks are implied, but the $\boldsymbol{N}$ marks are not the full marks: this indicates that we want to see some of the working, without specifying what.
- For consistency within the markscheme, $\boldsymbol{N}$ marks are noted for every part, even when these match the mark breakdown.
- If a candidate has incorrect working, which somehow results in a correct answer, do not award the $\boldsymbol{N}$ marks for this correct answer. However, if the candidate has indicated (usually by crossing out) that the working is to be ignored, award the $\boldsymbol{N}$ marks for the correct answer.

Implied and must be seen marks
Implied marks appear in brackets eg (M1).

- Implied marks can only be awarded if the work is seen or if implied in subsequent working (a correct final answer does not necessarily mean that the implied marks are all awarded). There are questions where some working is required, but as it is accepted that not everyone will write the same steps, all the marks are implied, but the $\mathbf{N}$ marks are not the full marks for the question.
- Normally the correct work is seen in the next line.
- Where there is an (M1) followed by $\mathbf{A 1}$ for each correct answer, if no working shown, one correct answer is sufficient evidence to award the (M1).


## Must be seen marks appear without brackets eg M1.

- Must be seen marks can only be awarded if the work is seen.
- If a must be seen mark is not awarded because work is missing (as opposed to MO or AO for incorrect work) all subsequent marks may be awarded if appropriate.


## 5 Follow through marks (only applied after an error is made)

Follow through (FT) marks are awarded where an incorrect answer (final or intermediate) from one part of a question is used correctly in subsequent part(s) or subpart(s). Usually, to award FT marks, there must be working present and not just a final answer based on an incorrect answer to a previous part. However, if the only marks awarded in a subpart are for the final answer, then FT marks should be awarded if appropriate. Examiners are expected to check student work in order to award FT marks where appropriate.

- Within a question part, once an error is made, no further $\boldsymbol{A}$ marks can be awarded for work which uses the error, but $\boldsymbol{M}$ and $\boldsymbol{R}$ marks may be awarded if appropriate. (However, as noted above, if an $\boldsymbol{A}$ mark is not awarded because work is missing, all subsequent marks may be awarded if appropriate).
- Exceptions to this rule will be explicitly noted on the markscheme.
- If the question becomes much simpler because of an error then use discretion to award fewer FT marks.
- If the error leads to an inappropriate value (eg probability greater than 1 , use of $r>1$ for the sum of an infinite GP, $\sin \theta=1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word "their" in a description, to indicate that candidates may be using an incorrect value.
- If a candidate makes an error in one part, but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the question says hence. It is often possible to use a different approach in subsequent parts that does not depend on the answer to previous parts.
- In a "show that" question, if an error in a previous subpart leads to not showing the required answer, do not award the final A1. Note that if the error occurs within the same subpart, the FT rules may result in further loss of marks.

If a candidate incorrectly copies information from the question, this is a mis-read (MR). A candidate should be penalized only once for a particular mis-read. Use the MR stamp to indicate that this is a misread. Do not award the first mark in the question, even if this is an $\boldsymbol{M}$ mark, but award all others (if appropriate) so that the candidate only loses one mark for the misread.

- If the question becomes much simpler because of the $\boldsymbol{M R}$, then use discretion to award fewer marks.
- If the $\boldsymbol{M R}$ leads to an inappropriate value (eg probability greater than 1 , use of $r>1$ for the sum of an infinite GP, $\sin \theta=1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does not constitute a misread, it is an error.

7 Discretionary marks (d)
An examiner uses discretion to award a mark on the rare occasions when the markscheme does not cover the work seen. In such cases the annotation DM should be used and a brief note written next to the mark explaining this decision.

8 Alternative methods
Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If in doubt, contact your team leader for advice.

- Alternative methods for complete parts are indicated by METHOD 1, METHOD 2, etc.
- Alternative solutions for parts of questions are indicated by EITHER . . . OR. Where possible, alignment will also be used to assist examiners in identifying where these alternatives start and finish.


## 9 Alternative forms

Unless the question specifies otherwise, accept equivalent forms.

- As this is an international examination, accept all alternative forms of notation.
- In the markscheme, equivalent numerical and algebraic forms will generally be written in brackets immediately following the answer.
- In the markscheme, simplified answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).

10 Calculators
A GDC is required for paper 2, but calculators with symbolic manipulation features (eg TI-89) are not allowed.

Calculator notation The mathematics SL guide says:
Students must always use correct mathematical notation, not calculator notation.
Do not accept final answers written using calculator notation. However, do not penalize the use of calculator notation in the working.

Style
The markscheme aims to present answers using good communication, eg if the question asks to find the value of $k$, the markscheme will say $k=3$, but the marks will be for the correct value 3 there is usually no need for the " $k=$ ". In these cases, it is also usually acceptable to have
another variable, as long as there is no ambiguity in the question, eg if the question asks to find the value of $p$ and of $q$, then the student answer needs to be clear. Generally, the only situation where the full answer is required is in a question which asks for equations - in this case the markscheme will say "must be an equation".

The markscheme often uses words to describe what the marks are for, followed by examples, using the eg notation. These examples are not exhaustive, and examiners should check what candidates have written, to see if they satisfy the description. Where these marks are $\boldsymbol{M}$ marks, the examples may include ones using poor notation, to indicate what is acceptable.

## 12 Candidate work

If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work.

Candidates are meant to write their answers to Section A on the question paper (QP), and Section B on answer booklets. Sometimes, they need more room for Section A, and use the booklet (and often comment to this effect on the QP), or write outside the box. That is fine, and this work should be marked.

The instructions tell candidates not to write on Section B of the QP. Thus they may well have done some rough work here which they assume will be ignored. If they have solutions on the answer booklets, there is no need to look at the QP. However, if there are whole questions or whole part solutions missing on answer booklets, please check to make sure that they are not on the QP, and if they are, mark those whole questions or whole part solutions that have not been written on answer booklets.

## 13. Diagrams

The notes on how to allocate marks for sketches usually refer to passing through particular points or having certain features. These marks can only be awarded if the sketch is approximately the correct shape. All values given will be an approximate guide to where these points/features occur. In some questions, the first $\boldsymbol{A 1}$ is for the shape, in others, the marks are only for the points and/or features. In both cases, unless the shape is approximately correct, no marks can be awarded (unless otherwise stated). However, if the graph is based on previous calculations, FT marks should be awarded if appropriate.

## 14. Accuracy of Answers

If the level of accuracy is specified in the question, a mark will be allocated for giving the final answer to the required accuracy. When this is not specified in the question, all numerical answers should be given exactly or correct to three significant figures.

Do not accept unfinished numerical final answers such as $3 / 0.1$ (unless otherwise stated). As a rule, numerical answers with more than one part (such as fractions) should be given using integers (eg 6/8). Calculations which lead to integers should be completed, with the exception of fractions which are not whole numbers. Intermediate values do not need to be given to the correct three significant figures. But, if candidates work with rounded values, this could lead to an incorrect answer, in which case award $A 0$ for the final answer. Where numerical answers are required as the final answer to a part of a question in the markscheme, the markscheme will show a truncated 6 sf value
the exact value if applicable, the correct 3 sf answer

## Section A

1. (a) attempt to substitute $x=1$
(M1)
eg $\quad f(1), 1^{2}+1+\frac{50}{1}$
52 (exact)
(b) -4.04932
-4.05
A2
N2 [2 marks]
(c) $(2.76649,28.4934)$

A(2.77, 28.5)
A1A1
N2
[2 marks]
Total [6 marks]
2. (a) (i) valid approach
eg correct value for $a$ or $b$ (or for $r$ or $r^{2}=0.962839$ seen in (ii))

$$
\begin{aligned}
& a=-9.84636, b=221.592 \\
& a=-9.85, b=222
\end{aligned}
$$

A1A1
N3

$$
\text { (ii) } \begin{gathered}
-0.981244 \\
r=-0.981
\end{gathered}
$$

A1 [4 marks]
(b) correct substitution into their equation
eg $\quad-9.85 \times 12+222$
103.435 ( 103.8 from 3 sf )

103 (hot chocolates)
(A1)
3. (a) evidence of summing probabilities to 1
eg $\quad q+4 p^{2}+p+0.7-4 p^{2}=1,1-4 p^{2}-p-0.7+4 p^{2}$
$q=0.3-p$
A1
N2
[2 marks]
(b) (i) correct substitution into $\mathrm{E}(X)$ formula
eg $\quad 0 \times(0.3-p)+1 \times 4 p^{2}+2 \times p+3 \times\left(0.7-4 p^{2}\right)$
valid approach to find when $\mathrm{E}(X)$ is a maximum
(M1)
eg max on sketch of $\mathrm{E}(X), 8 p+2+3 \times(-8 p)=0, \frac{-b}{2 a}=\frac{-2}{2 \times(-8)}$
$p=\frac{1}{8}(=0.125)($ exact $)\left(\right.$ accept $\left.x=\frac{1}{8}\right)$
A1
N3
(ii) 2.225
$\frac{89}{40}$ (exact), 2.23
A1
N1
4. (a) attempt to form composite (in any order)
eg $\quad f(\ln x), g\left(4-x^{3}\right)$
$(f \circ g)(x)=4-(\ln x)^{3} \quad$ A1
(b) (i) valid approach using GDC
eg

2.85056
2.85

A1
(ii) METHOD 1 - (using properties of functions)
recognizing inverse relationship
(M1)
eg $\quad f(g(2 a))=f\left(f^{-1}(2 a)\right)(=2 a)$
equating $2 a$ to their $x$ from (i)
eg $\quad 2 a=2.85056$
1.42528
$a=1.43 \quad$ A
METHOD 2 - (finding inverse)
interchanging $x$ and $y$ (seen anywhere)
eg $\quad x=4-y^{3}, f^{-1}(x)=\sqrt[3]{4-x}$
correct working
eg $\quad \sqrt[3]{4-2 a}=\ln (2 a)$, sketch showing intersection of $f^{-1}(2 x)$ and $g(2 x)$
1.42528
$a=1.43$
5. valid approach for expansion (must have correct substitution for parameters, but accept an incorrect value for $r$ ).
eg $\binom{9}{r}\left(3 x^{2}\right)^{9-r}\left(-\frac{k}{x}\right)^{r},\left(3 x^{2}\right)^{9}+\binom{9}{1}\left(3 x^{2}\right)^{8}\left(-\frac{k}{x}\right)^{1}+\binom{9}{2}\left(3 x^{2}\right)^{7}\left(-\frac{k}{x}\right)^{2}+\ldots$
valid attempt to identify correct term
eg $\quad 2(9-r)-r=6,\left(x^{2}\right)^{r}\left(x^{-1}\right)^{9-r}=x^{6}$
identifying correct term (may be indicated in expansion)
eg $\quad r=4, r=5$
correct term or coefficient in binominal expansion
(A1)
eg $\quad\binom{9}{4}\left(3 x^{2}\right)^{5}\left(-\frac{k}{x}\right)^{4}, 126\left(243 x^{10}\right)\left(\frac{k^{4}}{x^{4}}\right), 30618 k^{4}$
correct equation in $k$
eg $\quad\binom{9}{4}(243)\left(k^{4}\right) x^{6}=6048 x^{6}, 30618 k^{4}=6048$
$k=\frac{2}{3}$ (exact) 0.667 A1

Note: Do not award A1 if additional answers given.
6. (a) evidence of dividing terms (in any order)
eg $\frac{u_{1}}{u_{2}}, \frac{\frac{1}{4} a^{2}-3 a}{a}$
$r=\frac{1}{4} a-3$
(b) recognizing $|r|<1$ (must be in terms of $a$ )
(M1)
eg $\left|\frac{1}{4} a-3\right|<1,-1 \leq \frac{1}{4} a-3 \leq 1,-4<a-12<4$
$8<a<16$ [3 marks]
(c) correct equation
eg $\frac{a}{1-\left(\frac{1}{4} a-3\right)}=76, a=76\left(4-\frac{1}{4} a\right)$
$a=\frac{76}{5}(=15.2)$ (exact)

N3
7. (a) correct working for AC (seen anywhere)
eg $\tan \theta=\frac{\mathrm{AC}}{\mathrm{OA}}, \tan \theta=\frac{\mathrm{AC}}{1}$
$\mathrm{AC}=\tan \theta$
AG
(b) METHOD 1 (working with half the areas)
area of triangle OAC or triangle OBC
eg $\frac{1}{2} \times 1 \times \tan \theta$
correct sector area
eg $\frac{1}{2} \times \theta \times\left(1^{2}\right), \frac{1}{2} \theta$
correct approach using their areas to find the shaded area (seen anywhere) (A1)
eg $\quad \mathrm{A}_{\text {their triangle }}-\mathrm{A}_{\text {their sector }}, \frac{1}{2} \theta-\frac{1}{2} \tan \theta$
correct equation
eg $\frac{1}{2} \tan \theta-\frac{1}{2} \theta=\frac{1}{2} \theta, \tan \theta=2 \theta$
1.16556
1.17 A2

METHOD 2 (working with entire kite and entire sector)
area of kite OACB
eg $2 \times \frac{1}{2} \times 1 \times \tan \theta, \frac{1}{2} \times \frac{1}{\cos \theta} \times 2 \sin \theta$
correct sector area
eg $\quad \frac{1}{2} \times 2 \theta \times\left(1^{2}\right), \theta$
correct approach using their areas to find the shaded area (seen anywhere) (A1)
eg $\quad \mathrm{A}_{\text {kite OACB }}-\mathrm{A}_{\text {sector OADB }}, \theta-\tan \theta$
correct equation
A1
eg $\tan \theta-\theta=\theta, \tan \theta=2 \theta$
1.16556
1.17 A2

## Section B

8. (a) (i) valid approach
(M1)
eg $\quad h(0), 13+8 \cos \left(\frac{\pi}{18} \times 0\right)-6 \sin \left(\frac{\pi}{18} \times 0\right), 13+8 \times 1-6 \times 0$
21 (metres) A1
N2
(ii) valid approach to find the period (seen anywhere)
(M1)
eg $(36,21)$, attempt to find two consecutive max/min, 50.3130-14.3130

$$
\frac{2 \pi}{\pi / 18}, b=\frac{2 \pi}{\text { period }},
$$

36 (seconds) (exact)
(iii) correct approach
eg $\frac{60 \times 60}{36}, 1.6666$ rotations per minute
100 (rotations)
A1
N2
(b) correct substitution into equation (accept the use of $t$ )
eg

$$
4.06=13+8 \cos \left(\frac{\pi}{18} \times k\right)-6 \sin \left(\frac{\pi}{18} \times k\right)
$$

valid attempt to solve their equation
eg

11.6510
11.7

A1

## Question 8 continued

(c) METHOD 1
evidence of choosing the cosine rule or sine rule
(M1)
eg $\mathrm{AB}^{2}=\mathrm{OA}^{2}+\mathrm{OB}^{2}-2 \times \mathrm{OA} \times \mathrm{OB} \cos (\mathrm{AOB}), \frac{\sin (\mathrm{AOB})}{\mathrm{AB}}=\frac{\sin (\mathrm{OAB})}{\mathrm{OB}}$
correct working
(A1)
eg $\cos (\mathrm{AOB})=\frac{10^{2}+10^{2}-17.0^{2}}{2 \times 10 \times 10},-0.445, \frac{\sin (\mathrm{AOB})}{17.0}=\frac{\sin \left(\frac{\pi}{2}-\frac{1}{2} \mathrm{AOB}\right)}{10}$,

$$
\frac{\sin \mathrm{OAB}}{10}=\frac{\sin (\pi-2 \times \mathrm{OAB})}{17.0}
$$

2.03197, 116.423
2.03 (116 )

A1

## METHOD 2

attempt to find the half central angle
eg $\quad \sin \left(\frac{1}{2} \mathrm{AOB}\right)=\frac{\frac{1}{2} \mathrm{AB}}{\mathrm{OA}}$
correct working
eg $\quad 2 \times \sin ^{-1}\left(\frac{8.5}{10}\right)$
2.03197, 116.423
$2.03\left(116^{\circ}\right) \quad$ A1
continued...

Question 8 continued
METHOD 3valid approach to find fraction of period(M1)eg $\frac{k}{36}, \frac{11.6510}{36}$correct approach to find angle(A1)
eg $\frac{k}{36} \times 2 \pi$
$2.03348,116.510^{\circ}$ (2.04203 using 11.7)
2.03 ( $117^{\circ}$ ) ..... A1
N3[3 marks](d) recognizing rate of change is $h^{\prime}$(M1)eg $\quad h^{\prime}(k), h^{\prime}(11.6510), 0.782024$
-0.782024 ( -0.768662 from 3 sf )rate of change is $-0.782\left(\mathrm{~ms}^{-1}\right)$A1N2
( $-0.769\left(\mathrm{~ms}^{-1}\right)$ from 3 sf )
9. (a) 0.158655
$\mathrm{P}(15<W<30)=0.159$
A2
[2 marks]
(b) finding standardized value for 60
eg $\quad z=1.56322$
correct substitution using their $z$-value
eg $\quad \frac{60-50}{\sigma}=1.56322, \frac{60-50}{1.56322}=\sigma$
6.39703
$\sigma=6.40$
A1
N3
[3 marks]
(c) 0.217221
$\mathrm{P}(B<45)=0.217$
A2
N2
[2 marks]
(d) valid attempt to find one possible way of being on time (do not penalize incorrect use of strict inequality signs)
eg $W \leq 15$ and $B<60,15<W \leq 30$ and $B<45$
correct calculation for $\mathrm{P}(W \leq 15$ and $B<60)$ (seen anywhere)
eg $\quad 0.841 \times 0.941,0.7917$
correct calculation for $\mathrm{P}(15<W \leq 30$ and $B<45)$ (seen anywhere)
eg $\quad 0.159 \times 0.217,0.03446$
correct working
(A1)
eg $\quad 0.841 \times 0.941+0.159 \times 0.217,0.7917+0.03446$
0.826168
$\mathrm{P}($ on time $)=0.826$
(e) recognizing binomial with $n=183, p=0.826168$
eg $\quad X \sim \mathrm{~B}(183,0.826)$
151.188 ( 151.158 from 3 sf )

151
10. (a) METHOD 1
evidence of choosing the quotient rule
eg $\frac{v u^{\prime}-u v^{\prime}}{v^{2}}$
derivative of $6 x$ is 6 (must be seen in rule)
derivative of $x^{2}+4$ is $2 x$ (must be seen in rule)
correct substitution into the quotient rule
eg $\frac{6\left(x^{2}+4\right)-(6 x)(2 x)}{\left(x^{2}+4\right)^{2}}$
$f^{\prime \prime}(x)=\frac{24-6 x^{2}}{\left(x^{2}+4\right)^{2}}$

## METHOD 2

evidence of choosing the product rule
eg $v u^{\prime}+u v^{\prime}$
derivative of $6 x$ is 6 (must be seen in rule)
derivative of $\left(x^{2}+4\right)^{-1}$ is $-2 x\left(x^{2}+4\right)^{-2}$ (must be seen in rule)
correct substitution into the product rule
eg $\quad 6\left(x^{2}+4\right)^{-1}+(-1)(6 x)(2 x)\left(x^{2}+4\right)^{-2}$
$f^{\prime \prime}(x)=\frac{24-6 x^{2}}{\left(x^{2}+4\right)^{2}}$

AG [4 marks]
(b) METHOD 1 (2 ${ }^{\text {nd }}$ derivative)
valid approach
eg $\quad f^{\prime \prime}<0,24-6 x^{2}<0, n= \pm 2, x=2$

$$
n=2 \text { (exact) } \quad \text { A1 }
$$

METHOD 2 ( $1^{\text {st }}$ derivative)
valid attempt to find local maximum on $f^{\prime}$
eg sketch with max indicated, (2, 1.5), $x=2$

$$
n=2 \text { (exact) A1 }
$$

[2 marks]

Question 10 continued
(c) evidence of valid approach using substitution or inspection
eg $\quad \int 3(2 x) \frac{1}{u} \mathrm{~d} x, u=x^{2}+4, \mathrm{~d} u=2 x \mathrm{~d} x, \int 3 \times\left(\frac{1}{u}\right) \mathrm{d} u$

$$
\begin{equation*}
\int \frac{6 x}{\left(x^{2}+4\right)} \mathrm{d} x=3 \ln \left(x^{2}+4\right)+c \tag{A2}
\end{equation*}
$$

N3
(d) recognizing that area $=\int_{1}^{3} f(x) \mathrm{d} x$ (seen anywhere)
recognizing that their answer to (c) is their $f(x)$ (accept absence of $c$ )
eg $\quad f(x)=3 \ln \left(x^{2}+4\right)+c, f(x)=3 \ln \left(x^{2}+4\right)$
correct value for $\int_{1}^{3} 3 \ln \left(x^{2}+4\right) \mathrm{d} x$ (seen anywhere)
eg $\quad 12.4859$
correct integration for $\int_{1}^{3} c \mathrm{~d} x$ (seen anywhere)
$[c x]_{1}^{3}, 2 c$
adding their integrated expressions and equating to 19.6 (do not accept an expression which involves an integral)
eg $\quad 12.4859+2 c=19.6,2 c=7.114$
$c=3.55700$
$f(x)=3 \ln \left(x^{2}+4\right)+3.56$

